

2016 UQ/QAMT Problem Solving Competition - Year 7 & 8 Paper

Two hours allowed. All questions have equal value. Non-CAS calculators may be used.

Question 1

In 2016 the first day of lectures at the University of Queensland was Monday, February 29th. When is the next year in which there will be a February 29th falling on a Monday?

Question 2

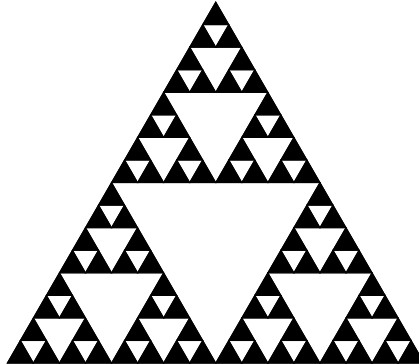
Suppose a parallelogram has corners $ABCD$, labelled clockwise (so AB is parallel to DC). Let P be a point inside the parallelogram with angles $\angle BAP = 42^\circ$ and $\angle CDP = 20^\circ$. What is the angle $\angle APD$?

Question 3

How can the numbers $1^2, 2^2, \dots, 15^2$ be arranged into 4 groups, such that each group has the same sum? Every number must be used exactly once but the groups can be of different sizes.

Question 4

How many triangles appear in the following diagram?



Question 5

Each letter Q, A, ... below corresponds to a different digit $0, 1, \dots, 9$ and the calculation is a valid addition. No initial digit (Q, T or R) can be 0. What is the value of M?

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