

# LECTURE 18 part 1: revision for mid-semester 1/2

\*  $z = x + iy = (x, y)$

"  $re^{i\theta}$

\*  $\mathbb{C}$  as a field (not ordered, can't be ordered)

\* Arg vs arg (vs  $\text{Arg}$ )

\*  $e^{i\theta} = \cos\theta + i\sin\theta$

\*  $e^{in\theta} = \cos n\theta + i\sin n\theta$

\* nth roots.

\* quadratic formula.

\*  $f^n$ 's as mappings (linear,  $1/z$ )

\* Möbius transformations

\* In partic.  $\left\{ \begin{array}{l} \text{lines} \\ \text{circles} \end{array} \right\} \rightarrow \left\{ \begin{array}{l} \text{lines} \\ \text{circles} \end{array} \right\}$

\* Riemann sphere

$\bar{\mathbb{C}}$ , Möbius transforms  $\bar{\mathbb{C}} \rightarrow \bar{\mathbb{C}}$ .

\* inverse  $f^n$ 's (inv of exp?)

\* log vs Log (vs  $\text{Log}$ )

\* branch, branch cut.

\* trig & hyperbolic  $f^n$ 's (inverses, zeros, identities)

\* bounded & unbounded  $f^n$ 's

\* basic topology on  $\mathbb{C}$  (& on  $\bar{\mathbb{C}}$ )

\* limits (included as)

\* continuity, differentiability

\* Cauchy-Riemann

rectangular  
polar  
Wirtinger

CR as necessary cond<sup>n</sup>s for  $\mathbb{C}$ -diff<sup>bility</sup>,  
covered sufficient cond<sup>n</sup>s.

\* Analytic f<sup>n</sup>s

(real analytic vs smooth f<sup>n</sup>s in  $\mathbb{R}^n$ )  
not examinable in mid-sem.